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Zbl 1068.46045

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On the manifold of tripotents in  $JB^*$ -triples. (English)

J. Math. Anal. Appl. 304, No. 1, 147-157 (2005).

<http://dx.doi.org/10.1016/j.jmaa.2004.09.009>

<http://www.sciencedirect.com/science/journal/0022247X>

Summary: The manifold of tripotents in an arbitrary  $JB^*$ -triple  $Z$  is considered, a natural affine connection is defined on it in terms of the Peirce projections of  $Z$ , and a precise description of its geodesics is given. Regarding this manifold as a fiber space by Neher's equivalence, the base space is a symmetric Kähler manifold when  $Z$  is a classical Cartan factor, and necessary and sufficient conditions are established for connected components of the manifold to admit a Riemann structure.

*Keywords* :  $JB^*$ -triples; Cartan factors; Grassmann manifolds; Banach-Lie algebras and groups; Riemann manifolds

*Classification* :

\*46L70 Nonassociative selfadjoint operator algebras

58B20 Geometric structures on infinite-dimensional manifolds