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1. Determine the Prüfer code of the following labeled tree.

2. Using the Havel-Hakimi-algorithm, decide whether the following sequence can be realized by a simple graph or not: $5,5,5,4,2,1,1,1$.
3. Find a minimum cost spanning in the following weighted graph using Kruskal's algorithm:

4. Consider the network in the figure ( $s$ is the source, $t$ is the sink; and the label of an edge $e$ is $f(e) / c(e)$ where $f$ is a flow, $c$ is the capacity function).

a) Check that the flow $f$ in the figure is feasible.
b) Determine the value of the flow $f$.
c) Find an augmenting path (with respect to $f$ ), and augment the flow using the path.
5. Let $G$ be the graph seen in the figure below.
a) Determine $\kappa(G)$, i.e. find the largest number $k$ for which $G$ is $k$-connected.
b) Determine $\lambda(G)$, i.e. find the largest number $l$ for which $G$ is $l$-edge-connected.

