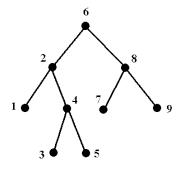
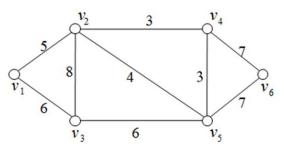
Name: .....

1. Determine the Prüfer code of the following labeled tree.

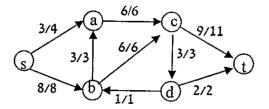


**2.** Using the Havel–Hakimi-algorithm, decide whether the following sequence can be realized by a simple graph or not: 5, 5, 5, 4, 2, 1, 1, 1.

**3.** Find a minimum cost spanning in the following weighted graph using Kruskal's algorithm:



**4.** Consider the network in the figure (s is the source, t is the sink; and the label of an edge e is f(e)/c(e) where f is a flow, c is the capacity function).



- a) Check that the flow f in the figure is feasible.
- b) Determine the value of the flow f.
- c) Find an augmenting path (with respect to f), and augment the flow using the path.

**5.** Let G be the graph seen in the figure below.

- a) Determine  $\kappa(G)$ , i.e. find the largest number k for which G is k-connected.
- b) Determine  $\lambda(G)$ , i.e. find the largest number *l* for which *G* is *l*-edge-connected.

