## 5. Eulerian tour

1. Which of the following graphs contains an Eulerian tour?

2. The graph $G$ is defined as follows. The vertex set of $G$ is $\{1, \ldots, 100\}$, and the numbers (vertices) $i$ and $j$ are adjacent if and only if $1 \leq|i-j| \leq 2$. Does $G$ contains an Eulerian tour?
3. Which of the following figures can be drawn without lifting the pencil?

4. A connected graph $G$ is given. Prove that there exists a closed walk in $G$ which visits every edge of $G$ exactly twice.
5. Prove that if exacty two vertices has odd degree in $G$, then there exists a path between these two vertices in $G$.
6. ${ }^{+}$A domino consists of two squares glued together. Every square contains the number 0,1 , $2,3,4,5$ or 6 (denoted by dots). Every possible unordered pair of these numbers appears on exactly one domino, so the total number of dominoes is $7+\binom{7}{2}=28$. Is it possible to put all the dominoes in a row so that the numbers on any two adjacent dominoes, written on their common side, coincide?
