ERDŐS-KO-RADO PROPERTY OF TRANSITIVE PERMUTATION GROUPS

Ademir Hujdurović

University of Primorska (Slovenia)

The Erdős-Ko-Rado theorem is one of the central results in extremal combinatorics. It gives a bound on the size of a family of intersecting k-subsets of a set and classifies the families satisfying the bound. In this presentation I will talk about the extension of Erdős-Ko-Rado theorem to transitive permutation groups.

Given a transitive permutation group G acting on a set V, two permutations $g, h \in G$ are said to be *intersecting* if there exists $v \in V$ such that g(v) = h(v). Intersecting set of permutations is a set in which any two permutations are intersecting. Obvious example of an intersecting set is a point stabilizer G_v . If G_v is the largest intersecting set in G, then G is said to have the Erdős-Ko-Rado (EKR)-property. The intersection density $\rho(G)$ of a transitive permutation group G is the maximum value of the quotient $|\mathcal{F}|/|G_v|$ where \mathcal{F} runs over all intersecting sets in G.

I will present some known and some new results on the maximum sizes of intersecting sets in certain transitive permutation groups. I will show how the existence of certain cyclic codes was used for construction of transitive groups of degree a product of two odd primes which don't have the EKR property. I will also present several results regarding intersection density of transitive groups having small point stabilizer.

Based on joint work with Klavdija Kutnar, Bojan Kuzma, Istvan Kovacs, Dragan Marušič, Štefko Miklavič and Marko Orel.