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	<pre> *-----* / *-----* *-----* / *-----* MuPAD 2.0.0 -- The Open Computer Algebra System Copyright (c) 1997 - 2000 by SciFace Software All rights reserved. UNREGISTERED VERSION Please contact info@sciface.com to register. >> # Elemi függvények # >> exp(ln(2)); 2 x >> exp(2*ln(x)); 2 x >> sin(arcsin(2)); 2 x >> sin(-x); -sin(x) >> sin(PI/2); 1 >> cos(x+PI); -cos(x) >> cos(x+2*PI); cos(x) >> sin(arctan(2)); 1/2 2 5 ----- 5 >> DIGITS:=100: sin(0.1); 0.099833416646828152306814198410622026989915388017982259992766861561651744\ 28329242760966244380406303627 >> DIGITS:=50: sin(1); sin(1) >> DIGITS:=50: sin(1.0); DIGITS:=10: 0.84147098480789650665250232163029899962256306079837 >> arccos(cos(3)); 3 >> log(10,100); 2 >> sign(5); 1 >> assume(x<0): sign(x*y)*sign(x); sign(y) >> trunc(5.5); </pre>	

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	<pre> >> trunc(-5.5); 5 >> round(5.5); -5 >> round(-5.5); 6 >> floor(5.5); -6 >> floor(-5.5); 5 >> frac(1.234); -6 >> frac(-1.234); 0.234 >> sqrt(x); 0.766 >> binomial(20,10); 1/2 x 184756 >> expand((a+b)^20); 20 20 19 19 2 18 3 17 4 16 a + b + 20 a b + 20 a b + 190 a b + 1140 a b + 4845 a b + 5 15 6 14 7 13 8 12 15504 a b + 38760 a b + 77520 a b + 125970 a b + 9 11 10 10 11 9 12 8 167960 a b + 184756 a b + 167960 a b + 125970 a b + 13 7 14 6 15 5 16 4 77520 a b + 38760 a b + 15504 a b + 4845 a b + 17 3 18 2 1140 a b + 190 a b >> max(1,2,3); 3 >> min(1,2,3); 1 >> >> # Határérték # >> limit(sin(x)/x,x=0); 1 >> limit((abs(x)-abs(0))/(x-0),x=0); -1 >> limit((abs(x)-abs(0))/(x-0),x=0,Left); -1 </pre>	

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>>	<code>^[[4m^[[0m ^[[4m^[[0m ^[[4m^[[0m</code>	
	<code>^[[4m^[[1mlimit^[[0m -- compute a limit^[[0m</code>	
	<code>^[[4mIntroduction^[[0m</code>	
	<code>^[[1mlimit^[[0m^[[1m(f, x = x0)^[[0m computes the bidirectional limit $\lim(f(x), x = x0)$.</code>	
	<code>^[[1mlimit^[[0m^[[1m(f, x = x0, Left)^[[0m computes the one-sided limit $\lim(f(x), x = x0-)$.</code>	
	<code>^[[1mlimit^[[0m^[[1m(f, x = x0, Right)^[[0m computes the one-sided limit $\lim(f(x), x = x0+)$.</code>	
	<code>^[[4mCall(s)^[[0m</code>	
	<code>^[[1mlimit(f, x <= x0> <, dir>)^[[0m</code>	
	<code>^[[4mParameters^[[0m</code>	
	<code>^[[0m ^[[1mf^[[0m^[[0m -^[[0m an ^[[4marithmetical expression^[[0m representing a function in ^[[1mx^[[0m</code>	
	<code>^[[0m ^[[1mx^[[0m^[[0m -^[[0m an ^[[4midentifier^[[0m</code>	
	<code>^[[0m ^[[1mx0^[[0m^[[0m -^[[0m the limit point: an ^[[4marithmetical expression^[[0m, possibly ^[[1m^[[4minfinity^[[0m^[[0m or ^[[1m-infinity^[[0m</code>	
	<code>^[[4mOptions^[[0m</code>	
	<code>^[[0m ^[[1m^[[1mdir^[[0m^[[0m^[[0m -^[[0m either ^[[1mLeft^[[0m or ^[[1mRight^[[0m. This controls the direction of the limit computation.</code>	
	<code>^[[4mReturns^[[0m</code>	
	<code>an ^[[4marithmetical expression^[[0m, an interval of type ^[[1m^[[4mDom::Interval^[[0m^[[0m, an ^[[4mexpression^[[0m of type ^[[1m"limit"^[[0m, or ^[[1m^[[4mFAIL^[[0m^[[0m.</code>	
	<code>^[[4mSide Effects^[[0m</code>	
	<code>The function is sensitive to the environment variable ^[[1m^[[4mORDER^[[0m^[[0m, which determines the default number of terms in series computations (see ^[[1m^[[4mseries^[[0m^[[0m and example ^[[4m6^[[0m below).</code>	
	<code>^[[4mProperties^[[0m of identifiers set by ^[[1m^[[4massume^[[0m^[[0m are taken into account.</code>	
	<code>^[[4mOverloadable:^[[0m</code>	
	<code>^[[1mf^[[0m</code>	
	<code>^[[4mRelated Functions^[[0m</code>	
	<code>^[[1m^[[4masympt^[[0m^[[0m, ^[[1m^[[4mdiff^[[0m^[[0m, ^[[1m^[[4mdiscont^[[0m^[[0m, ^[[1m^[[4mint^[[0m^[[0m, ^[[1m^[[4mO^[[0m^[[0m, ^[[1m^[[4mseries^[[0m^[[0m, ^[[1m^[[4mtaylor^[[0m^[[0m</code>	

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	<code>^[[4mDetails^[[0m</code>	
	<code>o ^[[1mlimit^[[0m^[[1m(f, x = x0)^[[0m computes the bidirectional limit of ^[[1mf^[[0m when ^[[1mx^[[0m tends to ^[[1mx0^[[0m on the real axis. The limit point ^[[1mx0^[[0m may be omitted, in which case ^[[1mlimit^[[0m assumes ^[[1mx0 = 0^[[0m.</code>	
	<code>If the limit point ^[[1mx0^[[0m is infinity or -infinity, then the limit is taken from the left to infinity or from the right to -infinity, respectively.</code>	
	<code>If the left and right limits are different, then ^[[1m^[[4mundefined^[[0m^[[0m is returned; see example ^[[4m2^[[0m.</code>	
	<code>o ^[[1mlimit^[[0m^[[1m(f, x = x0, Left)^[[0m returns the limit when ^[[1mx^[[0m tends to ^[[1mx0^[[0m from the left. ^[[1mlimit^[[0m^[[1m(f, x = x0, Right)^[[0m returns the limit when ^[[1mx^[[0m tends to ^[[1mx0^[[0m from the right. See example ^[[4m2^[[0m.</code>	
	<code>o If the limit does not exist mathematically, but the system can assert that the function ^[[1mf^[[0m is bounded when ^[[1mx^[[0m approaches ^[[1mx0^[[0m, then a bounding interval, of type ^[[1m^[[4mDom::Interval^[[0m^[[0m, for ^[[1mf(x)^[[0m in a sufficiently small neighborhood of ^[[1mx0^[[0m is returned. This may happen, e.g., if ^[[1mf^[[0m oscillates infinitesimally fast in the neighborhood of ^[[1mx0^[[0m; see example ^[[4m4^[[0m. The boundaries are the limes inferior and the limes superior of ^[[1mf^[[0m for x -> x0.</code>	
	<code>o If the limit cannot be computed, then the system returns a symbolic ^[[1mlimit^[[0m call (see example ^[[4m3^[[0m).</code>	
	<code>o If ^[[1mf^[[0m contains parameters, then ^[[1mlimit^[[0m reacts to ^[[4mproperties^[[0m of those parameters set by ^[[1m^[[4massume^[[0m^[[0m; see example ^[[4m5^[[0m. If the limit cannot be computed without additional assumptions about the parameters, then ^[[1mlimit^[[0m indicates this by a warning.</code>	
	<code>o Internally, ^[[1mlimit^[[0m tries to determine the limit from a series expansion of ^[[1mf^[[0m around ^[[1mx = x0^[[0m computed via ^[[1m^[[4mseries^[[0m^[[0m. If the number of terms in the series expansion is too small to compute the limit, then ^[[1mlimit^[[0m returns ^[[1m^[[4mFAIL^[[0m^[[0m. In such a case, it may be necessary to increase the value of the environment variable ^[[1m^[[4mORDER^[[0m^[[0m in order to find the limit (see example ^[[4m6^[[0m).</code>	
	<code>^[[4mExample 1^[[0m</code>	
	<code>The following command computes $\lim((1 - \cos(x))/x^2, x=0)$:</code>	
	<code>>> limit((1 - cos(x))/x^2, x)</code>	

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	$1/2$ <p>A possible definition of e is given by the limit of the sequence $(1+1/n)^n$ for $n \rightarrow \infty$:</p> <pre>>> limit((1 + 1/n)^n, n = infinity)</pre> $\exp(1)$ <p>Here is a more complex example:</p> <pre>>> limit((exp(x*exp(-x))/(exp(-x) + exp(-2*x^2/(x+1)))) - exp(x))/x, x = infinity)</pre> $-\exp(2)$ <p>Example 2</p> <p>The bidirectional limit of $f(x)=1/x$ for $x \rightarrow 0$ does not exist:</p> <pre>>> limit(1/x, x = 0)</pre> <p>undefined</p> <p>You can compute the one-sided limits from the left and from the right by passing the options <code>left</code> and <code>right</code>, respectively:</p> <pre>>> limit(1/x, x = 0, Left), limit(1/x, x = 0, Right)</pre> $-\infty, \infty$ <p>Example 3</p> <p>If <code>limit</code> is not able to compute the limit, then a symbolic <code>limit</code> call is returned:</p> <pre>>> delete f: limit(f(x), x = infinity)</pre> $\text{limit}(f(x), x = \infty)$ <p>Example 4</p> <p>The function $\sin(x)$ oscillates for $x \rightarrow \infty$. The lower and upper limits are -1 and 1, respectively:</p>	

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	<pre>>> limit(sin(x), x = infinity)</pre> $[-1, 1]$ <p>In fact, for $x \rightarrow \infty$ the function $\sin(x)$ assumes every value in the returned interval infinitely often. This need not be the case in general.</p> <p>Example 5</p> <p><code>limit</code> is not able to compute the limit of x^n for $x \rightarrow \infty$ without additional information about the parameter n:</p> <pre>>> delete n: limit(x^n, x = infinity)</pre> <p>Warning: cannot determine sign of n [stdlib::limit::limitMRV]</p> $\lim_{x \rightarrow \infty} x^n$ <p>However, for $n > 0$ the limit exists and equals infinity. We use <code>assume</code> to achieve this:</p> <pre>>> assume(n > 0): limit(x^n, x = infinity)</pre> ∞ <p>Similarly, the limit is zero for $n < 0$:</p> <pre>>> assume(n < 0): limit(x^n, x = infinity)</pre> 0 <p>Example 6</p> <p>It may be necessary to increase the value of the environment variable <code>ORDER</code> in order to find the limit, as in the following example:</p> <pre>>> limit((sin(tan(x)) - tan(sin(x)))/x^7, x = 0)</pre> <p>Warning: ORDER seems to be not big enough for series \ computation [stdlib::limit::lterm]</p> FAIL <pre>>> ORDER := 8: limit((sin(tan(x)) - tan(sin(x)))/x^7, x)</pre>	

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	-1/30	
	<pre>^[[4mBackground^[[0m o If a limit cannot be computed, then ^[[1mlimit^[[0m issues a warning with a possible reason, as shown in examples ^[[4m5^[[0m and ^[[4m6^[[0m. You may wa nt to suppress these warnings when you call ^[[1mlimit^[[0m from within your own procedures. You can control this by means of the procedure ^[[1mstdlib::limit::printWarnings^[[0m. The calls ^[[1mstdlib::limit::printWarnings(TRUE)^[[0m and ^[[1mstdlib::limit::printWarnings(FALSE)^[[0m switch the warnings that ^[[1ml imit^[[0m issues on and off, respectively, and return the previous setting. The command ^[[1mstdlib::limit::printWarnings()^[[0m returns the current setting, which is ^[[1m^[[4mTRUE^[[0m^[[0m by default. o ^[[1mlimit^[[0m first tries a series computation to determine the limit. If t his fails, then an algorithm based on the thesis of Dominik Gruntz: ``On Computing Limits in a Symbolic Manipulation System'', Swiss Federal Institute of Technology, Zurich, Switzerland, 1995, is used. ^[[4mChanges^[[0m o ^[[1mlimit^[[0m may return an interval of type ^[[1m^[[4mDom::Interval^[[0m^[[0m. ----- ?limit >> >> # Szummáció # >> sum(1/n,n=1..infinity); >> sum(1/(n^2),n=1..infinity); infinity 2 PI ---</pre>	
	6	
	<pre>>> sum(1/(n^3),n=1..infinity); zeta(3) >> sum(1/(n^4),n=1..infinity); 4 PI ---</pre>	
	90	
	<pre>>> float(_plus(1/(n^3),n=1..1000)); Error: [_plus] >> DIGITS:=200: float(PI); DIGITS:=10: 3.141592653589793238462643383279502884197169399375105820974944592307816406\ 28620899862803482534211706798214808651328230664709384460955058223172535940\ 81284811174502841027019385211055596446229489549303819</pre>	

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	<pre>>> >> >> # Differenciálás # >> diff(E^x+c,x); exp(x) >> diff(x^n,x); n - 1 n x >> diff(2^x,x); x 2 ln(2) >> diff(sin(2*x),x); 2 cos(2 x) >> diff(%,x); -4 sin(2 x) >> diff(%,x); -8 cos(2 x) >> diff(%,x); 16 sin(2 x) >> diff(%,x); 32 cos(2 x) >> diff(x^100,x \$ 30); 70 7791097137057804874587232499277321440358327700684800000000 x >> >> # Integrálás # >> int(E^x,x); exp(x) >> int(x^3-3*x^2+2,x); 3 x 2 x - x + -- 4 >> int(1/(ln(x)*x),x); ln(ln(x)) >> int(sin(x)/x,x=1..2); Warning: While integrating, we will assume x has property [1, 2] of Type::\ Real instead of given property < 0. [intlib::defInt] Si(2) - Si(1) >> float(%); 0.6593299064 >> T:=series(sin(x)/x,x=0,10); 2 4 6 8 9 x x x x x 1 - -- + --- - ---- + ----- + O(x) 6 120 5040 362880 >> int(T,x);</pre>	

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```

          3      5      7      9      10
      x  -  - +  - - - - - - +  - - - - - + O(x )
      18    600   35280  3265920
>> int(T,x=1..2);
Warning: While integrating, we will assume x has property [1, 2] of Type::\
Real instead of given property < 0. [intlib::defInt]
Warning: While integrating, we will assume x has property [1, 2] of Type::\
Real instead of given property < 0. [intlib::defInt]

          9
      int(O(x ), x = 1..2) + 75366677/114307200
>> float(%);

          9
      int(O(x ), x = 1..2) + 0.6593344689
>>
>> # Sorbafejtés #
>> taylor(cos(x)/x,x=0,10);
Error: does not have a Taylor series expansion, try 'series' [taylor]
>> taylor(exp(x),x=0,10);

          2      3      4      5      6      7      8      9      10
      1 + x +  -  +  -  +  -  +  -  +  -  +  -  +  -  + O(x )
          2      6     24    120   720   5040  40320  362880

>>
>> # Gyökkeresés #
>> solve(x^4-x^2=1);

      { --      1/2      1/2      1/2 -- }
      { | x = -  ----- + 1) | }
      { --      2      2      2      -- }

>> f:=x^5-x^4-3*x^3+2*x+5;

          3      4      5
      2 x - 3 x  - x  + x  + 5
>> solve(f);

x in ]-infinity, 0[ intersect RootOf(2 X49 - 3 X493 - X494 + X495 + 5, X49)
>> numeric::solve(f);

{[x = -1.472991017], [x = 1.568770674], [x = 1.906476185],
 [x = - 0.5011279209 - 0.9401206818 I],
 [x = - 0.5011279209 + 0.9401206818 I]}
>> quit

```

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```
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```

```
Eltérés a(z) 1. lépésben: -0.858407346410206884  
Eltérés a(z) 10. lépésben: 0.099753034660389872  
Eltérés a(z) 100. lépésben: 0.009999750031239429  
Eltérés a(z) 1000. lépésben: 0.000999999749998981  
Eltérés a(z) 10000. lépésben: 0.000099999999758627  
Eltérés a(z) 100000. lépésben: 0.000010000000073340
```

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GNU Octave, version 2.0.16 (i386-suse-linux-gnu). Copyright (C) 1996, 1997, 1998, 1999, 2000 John W. Eaton. This is free software with ABSOLUTELY NO WARRANTY. For details, type 'warranty'.		
i=1 n=6 m=0.866025403784438597 i=2 n=12 m=0.965925826289068312 i=3 n=24 m=0.991444861373810382 i=4 n=48 m=0.997858923238603479 i=5 n=96 m=0.999464587476365685 i=6 n=192 m=0.999866137909561803 i=7 n=384 m=0.999966533917401090 i=8 n=768 m=0.999991633444350603 i=9 n=1536 m=0.999997908358900123 i=10 n=3072 m=0.999999477089588362 i=11 n=6144 m=0.999999869272388597 i=12 n=12288 m=0.999999967318096594 i=13 n=24576 m=0.999999991829524149 i=14 n=49152 m=0.999999997957381037 i=15 n=98304 m=0.999999999489345259 i=16 n=196608 m=0.999999999872336343 i=17 n=393216 m=0.999999999968084086 i=18 n=786432 m=0.999999999992021049 i=19 n=1572864 m=0.999999999998005262 i=20 n=3145728 m=0.999999999999501288 i=21 n=6291456 m=0.999999999999875322 i=22 n=12582912 m=0.999999999999968914 i=23 n=25165824 m=0.999999999999992228 i=24 n=50331648 m=0.999999999999998002 i=25 n=100663296 m=0.999999999999999556 i=26 n=201326592 m=0.999999999999999889 i=27 n=402653184 m=1.000000000000000000 i=28 n=805306368 m=1.000000000000000000 i=29 n=1610612736 m=1.000000000000000000		

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```
i=1 n=6 PI-T=0.543516442236477104
i=2 n=12 PI-T=0.141592653589793560
i=3 n=24 PI-T=0.035764112359544242
i=4 n=48 PI-T=0.008964040308555354
i=5 n=96 PI-T=0.002242450542925489
i=6 n=192 PI-T=0.000560702699283322
i=7 n=384 PI-T=0.000140181304330689
i=8 n=768 PI-T=0.000035045677935219
i=9 n=1536 PI-T=0.000008761441474547
i=10 n=3072 PI-T=0.000002190361742205
i=11 n=6144 PI-T=0.000000547590521371
i=12 n=12288 PI-T=0.000000136897635450
i=13 n=24576 PI-T=0.000000034224409085
i=14 n=49152 PI-T=0.000000008556102049
i=15 n=98304 PI-T=0.000000002139024957
i=16 n=196608 PI-T=0.000000000534755795
i=17 n=393216 PI-T=0.000000000133688616
i=18 n=786432 PI-T=0.000000000033421266
i=19 n=1572864 PI-T=0.000000000008355094
i=20 n=3145728 PI-T=0.000000000002088552
i=21 n=6291456 PI-T=0.000000000000521805
i=22 n=12582912 PI-T=0.000000000000130118
i=23 n=25165824 PI-T=0.000000000000031974
i=24 n=50331648 PI-T=0.000000000000007550
i=25 n=100663296 PI-T=0.000000000000001776
i=26 n=201326592 PI-T=0.000000000000000888
i=27 n=402653184 PI-T=0.000000000000000000
i=28 n=805306368 PI-T=0.000000000000000000
i=29 n=1610612736 PI-T=0.000000000000000000
```


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Eltérés a(z) 1. lépésben: -0.858407346410206884
 Eltérés a(z) 2. lépésben: 0.474925986923126153
 Eltérés a(z) 3. lépésben: -0.325074013076873669
 Eltérés a(z) 4. lépésben: 0.246354558351697506
 Eltérés a(z) 5. lépésben: -0.198089886092747136
 Eltérés a(z) 6. lépésben: 0.165546477543616621
 Eltérés a(z) 7. lépésben: -0.142145830148691310
 Eltérés a(z) 8. lépésben: 0.124520836517975297
 Eltérés a(z) 9. lépésben: -0.110773281129083578
 Eltérés a(z) 10. lépésben: 0.099753034660389872
 Eltérés a(z) 11. lépésben: -0.090723155815800816
 Eltérés a(z) 12. lépésben: 0.083189887662459938
 Eltérés a(z) 13. lépésben: -0.076810112337540204
 Eltérés a(z) 14. lépésben: 0.071338035810607714
 Eltérés a(z) 15. lépésben: -0.066592998672150738
 Eltérés a(z) 16. lépésben: 0.062439259392365276
 Eltérés a(z) 17. lépésben: -0.058772861819755828
 Eltérés a(z) 18. lépésben: 0.055512852465958495
 Eltérés a(z) 19. lépésben: -0.052595255642149397
 Eltérés a(z) 20. lépésben: 0.049968846921953247
 Eltérés a(z) 21. lépésben: -0.047592128687802937
 Eltérés a(z) 22. lépésben: 0.045431127126150717
 Eltérés a(z) 23. lépésben: -0.043457761762738301
 Eltérés a(z) 24. lépésben: 0.041648621215985226
 Eltérés a(z) 25. lépésben: -0.039984031845239354
 Eltérés a(z) 26. lépésben: 0.038447340703780419
 Eltérés a(z) 27. lépésben: -0.037024357409427111
 Eltérés a(z) 28. lépésben: 0.035702915317845640
 Eltérés a(z) 29. lépésben: -0.034472523278645362
 Eltérés a(z) 30. lépésben: 0.033324086890845983
 Eltérés a(z) 31. lépésben: -0.032249683600957368
 Eltérés a(z) 32. lépésben: 0.031242379891105898
 Eltérés a(z) 33. lépésben: -0.030296081647355422
 Eltérés a(z) 34. lépésben: 0.029405410889958183
 Eltérés a(z) 35. lépésben: -0.028565603602795253
 Eltérés a(z) 36. lépésben: 0.027772424566218756
 Eltérés a(z) 37. lépésben: -0.027022095981726224
 Eltérés a(z) 38. lépésben: 0.026311237351607009
 Eltérés a(z) 39. lépésben: -0.025636814596444957
 Eltérés a(z) 40. lépésben: 0.024996096795959932
 Eltérés a(z) 41. lépésben: -0.024386619253422559
 Eltérés a(z) 42. lépésben: 0.023806151830914946
 Eltérés a(z) 43. lépésben: -0.023252671698496652
 Eltérés a(z) 44. lépésben: 0.022724339795756165
 Eltérés a(z) 45. lépésben: -0.022219480428963045
 Eltérés a(z) 46. lépésben: 0.021736563527080754
 Eltérés a(z) 47. lépésben: -0.021274189161091250
 Eltérés a(z) 48. lépésben: 0.020831073996803617
 Eltérés a(z) 49. lépésben: -0.020406039405258092
 Eltérés a(z) 50. lépésben: 0.019998000998782128

már 09, 02 0:00

pi-idok.out

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```

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>> // Borwein kvadratikus algoritmus
>>
>> N:=6:
>> DIGITS:=500:
>>
>> a:=sqrt(2): b:=0: p:=2+sqrt(2):
>> for i from 1 to N do
>>   uj_a:=(sqrt(a)+1/sqrt(a))/2:
>>   uj_b:=(sqrt(a)*(1+b))/(a+b):
>>   uj_p:=p*uj_b*(1+uj_a)/(1+uj_b):
>>   a:=uj_a:
>>   b:=uj_b:
>>   p:=uj_p:
>>
>> elteres:=float(p-PI):
>> tizedesjegy_pontossag:=trunc(abs(trunc(log(10,elteres)))):
>> print(Unquoted, "Eltérés: ").
>>   expr2text(tizedesjegy_pontossag).
>>   " tizedesjegy."):
>> end_for;

```

Eltérés: 2 tizedesjegy.

Eltérés: 8 tizedesjegy.

Eltérés: 18 tizedesjegy.

Eltérés: 40 tizedesjegy.

Eltérés: 83 tizedesjegy.

Eltérés: 170 tizedesjegy.

>> quit

```

real    0m22.197s
user    0m21.770s
sys     0m0.370s

```

```

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```

```

>> // Borwein kvartikus algoritmus
>>
>> N:=5:
>> DIGITS:=1000:
>>
>> a:=6-4*sqrt(2): y:=sqrt(2)-1:

```

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pi-idok.out

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```

>> for i from 0 to N-1 do
>>   uj_y:=(1-(1-y^4)^(1/4))/(1+(1-y^4)^(1/4)):
>>   uj_a:=a*((1+uj_y)^4)-2^(2*i+3)*uj_y*(1+uj_y+uj_y^2):
>>   y:=uj_y:
>>   a:=uj_a:
>>   p:=1/a:
>>
>> elteres:=float(p-PI):
>> tizedesjegy_pontossag:=trunc(abs(trunc(log(10,elteres)))):
>> print(Unquoted, "Eltérés: ").
>>   expr2text(tizedesjegy_pontossag).
>>   " tizedesjegy."):
>> end_for;

```

Eltérés: 8 tizedesjegy.

Eltérés: 40 tizedesjegy.

Eltérés: 170 tizedesjegy.

Eltérés: 693 tizedesjegy.

Eltérés: 997 tizedesjegy.

```

>>
>> quit

```

```

real    0m34.248s
user    0m33.830s
sys     0m0.310s

```

```

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```

```

>> // Ooura kvadratikus algoritmus a PI kiszámítására.
>> // A módszer a Gauss-Legendre-féle számtani-mértani közép (AGM) gyorsított
>> // változata; az eredeti programban a szorzásokat gyors
>> // Fourier-transzformációval (FFT) végzik (ami további gyorsítás).
>> // Copyright (C) 1999 Takuya Ooura <ooura@mmm.t.u-tokyo.ac.jp>
>> // http://momonga.t.u-tokyo.ac.jp/~ooura/fft.html
>>
>> DIGITS:=1000: // Itt kell megadni a pontosságot.
>> ELTERES:=10^(-DIGITS): //
>> Sqrt_Sqrt_Elteres:=sqrt(sqrt(ELTERES)): //
>> n:=1: //
>>
>>   c := sqrt(0.125):
>>   a := 1 + 3 * c:
>>   b := sqrt(a):
>>   e := b - 0.625:
>>   b := 2 * b:
>>   c := e - c:
>>   a := a + e:
>>   npow := 4:
>>   while e > Sqrt_Sqrt_Elteres do
>>     npow := 2 * npow:
>>     e := (a + b) / 2:

```


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i=1 n=6 m=.86602540378443864676372317075293618347140262690519031402790348972\ 5966508454400018540573093378624287 x=1 PI-T=.54351644223647729817147387102069433378296151865953487889123412\ 3129916880923008943006315545206244203		
i=2 n=12 m=.96592582628906828674974319972889736763390483900840455040234307631\ 0423213979855516347561741858070452 x=.51763809020504152469779767524809665669813780263986102762800641463\ 0113949497603993844735949388499330 PI-T=.14159265358979323846264338327950288419716939937510582097494459\ 2307816406286208998628034825342117070		
i=3 n=24 m=.99144486137381041114455752692856287127773827444810227145877460352\ 8922068405082531763265433453277397 x=.26105238444010318309681245579097802038748140962346450378123389667\ 0265650459647259228480737984584243 PI-T=.035764112359544090275833179092294400834258353593965520690610\ 4527132709300585035559619129011121120		
i=4 n=48 m=.99785892323860350673806979127277760453186639632596641807472562927\ 4187850828698111037956547626966877 x=.13080625846028613363063111755035088288126460789010803566397530149\ 2693814892777930572416034523039976 PI-T=.00896404030855504130089391378776663954739248389353177560013783\ 2264628600770441887886265969527106256		
i=5 n=96 m=.99946458747636564442983644624285994588364095315313089603368742859\ 9674458291480489070820060615630369 x=.06543816564355228412731985263457625222992525450339239375619176751\ 4637470426534785459604967089728326 PI-T=.00224245054292603132749656207108169504681881001251296503953735\ 6483164848859538664890049996789158120		
i=6 n=192 m=.99986613790956178286274714906010002195345847142775142566570436111\ 7678718332025681806890704453565826 x=.03272346325297356328594384696834610047132981567239244974814148723\ 7746659648045140570847433469849730 PI-T=.00056070269928360035129045681984277716075718321227092067773975\ 1605217825812539296566996405035159048		
i=7 n=384 m=.99996653391740110345760381057913911237003239152400201555378732091\ 3251507865987093466996694261615110 x=.01636227920787425857039824658921801844533529416452341952057948786\ 9395791650646528660662556483480802 PI-T=.00014018130433116301203407431827723894950709482543064515336181\ 7484137080073875503826681212236549320		

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i=8 n=768 m=.99999163344435064914755862056883470820631843513005534979804061014\ 6982405957798028383213196212535752 x=.00818120805246957918924210834302383685031261696817992854723965236\ 1223834891446872068405136594911429 PI-T=.00003504567793559294618003814964334269279291978660927302368292\ 1383824409362075495780823980513831880		
i=9 n=1536 m=.99999790835890018104166372432685047011985442966963796400028652886\ 5271534387576238320830495121637079 x=.00409061258232819022882611784626426005671130508942161074227241896\ 9167503098218319552244744665660570 PI-T=.00000876144147482979367377955834953367712448359401325883491808\ 5597863807970610124360462372896212424		
i=10 n=3072 m=.99999947708958832761109823746401407779555602264324535182230850229\ 5128091128280785921170509203640298 x=.00204530736067660908238592229206387848510904769203534158371388824\ 5273331322007767142830480620072408 PI-T=.00000219036174314272418487734855116064288709069930877090972682\ 3987174026854539582504070922115054280		
i=11 n=6144 m=.99999986927238853704857515517161734697783685384035148725450231910\ 2694748968570675021677998522479114 x=.00102265381402739500247163869946902080272386682694276940575245689\ 8332487164632400376503588263738954 PI-T=.00000054759052168791786674266938553106967214440882114839041224\ 7567979495682278667240416592913844424		
i=12 n=12288 m=.99999996731809660020873887214910799212477104987677524490954984855\ 3649378822556495841909467488782913 x=.000511326923724834628123299041677729802119501834726478547125933748\ 2095516552932735964095631620218256 PI-T=.00000013689763579086976929851067097822945050700691820650339700\ 0630415836535475042009011679142354120		
i=13 n=24576 m=.99999999182952411667384663803013397534384502751287301637915404800\ 1048780389112773181329855767815864 x=.00025566346395130948052344901602532864686870304453467621730677964\ 0752647275554860534356069073112171 PI-T=.00000003422440928327309407121418384197497667378026388555757510\ 2312962705067479235224474150763103432		
i=14 n=49152 m=.99999999795738102708231552524588538297227930747251410367402745375\ 3971026542949376732184460524640016 x=.00012783173223676626186947646649138260988152781056255781673371926\ 3849165602625460130474715776617413 PI-T=.0000000855610234179050187436026447147454638813300446270923636\ 6739286684268082752460658054996493512		

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i=15 n=98304 m=.99999999948934525664019474785353706261343768748187857046032191171\ 0880362435970386388089786016708618 x=.00006391586615102207116070807251821846928420566418226833293283142\ 8121132542711501922590836328451701 PI-T=.00000000213902558675838974278728386374874192698968491692705996\ 3950722556162900832081419899607491784		
i=16 n=196608 m=.9999999987233631415189967862122304051682339686835924045669061473\ 4928158954721742046647376496906109 x=.0000319579330795909031093815425579333263503358446685194730153233\ 1929528365772989529067714664526266 PI-T=.00000000053475639677152020286402868193989259348825272066041423\ 7297909666930466499443247610061546696		
i=17 n=393216 m=.9999999996808407853746560663390442836378158635102740491164743804\ 9351972880568262872244496202009079 x=.00001597896654030543499584362445350196006406104280692607674654698\ 0670958234914661662839321667722200 PI-T=.00000000013368909919800022366442455284282791194569199344511023\ 4307459937338246333155412453657175240		
i=18 n=786432 m=.9999999999202101963433456959463826986819401995350055251289058485\ 2827106374053887731010152637630099 x=.00000798948327021646542806668183879235631019681169477246348191864\ 5364721086824765902504069028704743 PI-T=.00000000003342227479982006672538951992225589519098372398983581\ 6552059756184408791114680396210857160		
i=19 n=1572864 m=.9999999999800525490858165289466969867207322580271743629306828098\ 2591442829725410670919397800679915 x=.00000399474163511620120530147346356461485004455676682492653080263\ 0979610315687865210185461784346668 PI-T=.00000000000835556869997501735692770532681989200345682046882253\ 6573649529399059879588027721842648264		
i=20 n=3145728 m=.9999999999950131372714528887966805780632370590547466559830610837\ 5972574180527769713468547664336222 x=.00000199737081755909666405925404488658903363571572547377195911130\ 7678422159435141726244357721880529 PI-T=.00000000000208889217499500438145569844692853212744519950276990\ 5750916619246996022054953308273468616		
i=21 n=6291456 m=.9999999999987532843178631444841705402175612885485402178834123760\ 0675803340067844102572845624808516 x=.00000099868540877967283970569170986518056233278254800139575240199\ 4414131573869502687735474268398585 PI-T=.0000000000005222304374882922300291039676302054352696227929675\ 4414131573869502687735474268398585		

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1994025028491452891022572848536315080		
i=22 n=12582912 m=.9999999999996883210794657812638551597855984353287759923365203632\ 7008895209545202976003140869391035 x=.00000049934270438985198331235394158794637574452005163238561622949\ 1605364387787838330137800767018661 PI-T=.00000000000013055576093721218872816421119002021577116356292350\ 7930528800923258113890041779079570632		
i=23 n=25165824 m=.999999999999220802698664450123895727420977504645635502646961534\ 4503242757906208722145871905695479 x=.00000024967135219492793708861548164863083528480050429414620649761\ 9640108500310109371363024819123382 PI-T=.00000000000003263894023430335236813084105425341222354143421225\ 4788406672164019823180586453360927944		
i=24 n=50331648 m=.999999999999805200674666112341240046102555345081310469767343260\ 4807475446605148537502236727643590 x=.00000012483567609746421172336255468185819030616389052416717182657\ 6744164674337444248823774302175004 PI-T=.00000000000000815973505857585716616332202971628624198948156845\ 1350886552207278762366786153711887560		
i=25 n=100663296 m=.999999999999951300168666528073451643666095766052816320573316371\ 4801924619047356141900529540145714 x=.00000006241783804873213625906312907314414694658977754689172890296\ 6849279417149026395476057937391809 PI-T=.00000000000000203993376464396548367399374281528864702820955572\ 6166595012847633287317297547002733768		
i=26 n=201326592 m=.999999999999987825042166632017621762925302499534375168674982233\ 8077164621358673883237636084383084 x=.00000003120891902436607192920429600309964886031266085579006387133\ 9062187334749823040426615335770047 PI-T=.00000000000000050998344116099144542682113791548664782771939097\ 8707138816326129188888616809553421512		
i=27 n=402653184 m=.999999999999996956260541658004359118981874284758507071836129123\ 5103074359212235999796347979584938 x=.00000001560445951218303643956123943486579303830946734590076137071\ 1513827585467290174658678939280714 PI-T=.00000000000000012749586029024786601347545336710109730763543465\ 8981731033763542914286902889843483848		
i=28 n=805306368 m=.99999999999999239065135414501086884636127862431786818041902429\ 3769385489015158272337012399131811 x=.0000000780222975609151827915050614659739327282312314419213435000\ 5403842099828033627479586676853464		

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PI-T=.00000000000000003187396507256196679441699889728962036400434689\ 8239158688027869882060328038088795336		
i=29 n=1610612736 m=.9999999999999999809766283853625271540214698171310581363423524658\ 4329934733336333501565456041685523 x=.00000000390111487804575914699648887694425875179664923589163142535\ 3327666436522276436403730188593080 PI-T=.00000000000000000796849126814049171679475819654205181718949831\ 8080487402693645273281446368993305800		
i=30 n=3221225472 m=.9999999999999999952441570963406317873744653680684060001659554068\ 8451637387488241517319412683695315 x=.00000000195055743902287957442589891392782464098322741904183452748\ 5589166042258096929738223197487770 PI-T=.000000000000000000199212281703512293033559632864924087622899317\ 2535905149298116728405610012494226632		
i=31 n=6442450944 m=.99999999999999999988110392740851579467729349616287040916631080688\ 3908460819275420723345521896385031 x=.00000000097527871951143978732890626639587422864790677350546878071\ 1133423077439001986863590209121103 PI-T=.00000000000000000049803070425878073265495575588191821420211262\ 5016536801172050122171679180248278216		
i=32 n=12884901888 m=.99999999999999999997027598185212894866888161541329011848919969098\ 6505704036935276484570048218240701 x=.00000000048763935975571989367894773437693235284413627643353924138\ 6579918752271668636581344305705920 PI-T=.00000000000000000012450767606469518316817998107795505324745933\ 5900217264559865399042446277835973832		
i=33 n=25769803776 m=.99999999999999999999256899546303223716719279393910831188465109190\ 6324171668508142198527618921499721 x=.00000000024381967987785994684128569233584058123711119494820572430\ 3728649628315411284128963002165318 PI-T=.00000000000000000003112691901617379579232256040120598204292892\ 5810800492534010366453280064389735624		
i=34 n=51539607552 m=.999999999999999999999814224886575805929179647286513868936255971784\ 3290311534226478333973254680682246 x=.00000000012190983993892997342086932431134209122043661067557410939\ 1655478342719013978179575328258498 PI-T=.00000000000000000000778172975404344894809798792103382168142382\ 9272244665171839333875214100328309960		
i=35 n=103079215104 m=.99999999999999999999953556221643951482294901036505727305260223846\ 4901722164522128469837379248981677 x=.00000000006095491996946498671046297192359877068545345171015976479\ 1015976479		

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7316830803878823909632285633035077 PI-T=.0000000000000000000194543243851086223702558121905422580602418\ 3620529737764321000639093972958930120		
i=36 n=206158430208 m=.99999999999999999999988389055410987870573724585056260580764820392\ 8197717917947076324610687119261097 x=.00000000003047745998473249335523502468279035097713111976794487129\ 2485651776264293776756279910125422 PI-T=.0000000000000000000048635810962771555925646306968829210061031\ 0071517142620448705392081579155612872		
i=37 n=412316860416 m=.99999999999999999999997097263852746967643431104134679442344315375\ 1535468391463681217564549222310754 x=.00000000001523872999236624667761795468151904619286610914234050926\ 2069389807432558287927516723998684 PI-T=.00000000000000000000012158952740692888981412000272986900322159\ 4028629586517307902270895293924861128		
i=38 n=824633720832 m=.99999999999999999999999274315963186741910857773400583254158148236\ 0976553450972694158596018994931038 x=.00000000000761936499618312333880903263327500693447062322906813727\ 0641082874019774958624678706265907 PI-T=.0000000000000000000003039738185173222245353026538920449943471\ 2039084778817652557494232979742876872		
i=39 n=1649267441664 m=.99999999999999999999999818578990796685477714443185577900637791396\ 0437428274204662793750546406636366 x=.00000000000380968249809156166940452322820193894699000769679011251\ 0197217042060041570691368863181549 PI-T=.0000000000000000000000759934546293305561338258289147220289801\ 0105516741847407246709464661836653768		
i=40 n=3298534883328 m=.9999999999999999999999954644747699171369428610786108980603088745\ 0746437641367388712572322588908004 x=.00000000000095242062452289041735113134701645625860333755562416727\ 7386782256304091337261256700208239 PI-T=.00000000000000000000000189983636573326390334564675687874310196\ 0782363283498944028856223378032256200		
i=41 n=6597069766656 m=.9999999999999999999999988661186924792842357152695884401740999742\ 2726426945413952990522644453205526 x=.000000000000095242062452289041735113134701645625860333755562416727\ 7386782256304091337261256700208239 PI-T=.0000000000000000000000047495909143331597583641175384535404908\ 1336589827026564681669933362708440264		
i=42 n=13194139533312 m=.99999999999999999999999997165296731198210589288173930922722139157\ 8184095332284105671435573631359031		

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8257891738072583464174078006066399		
x=.00000000000000372039306454254069277785696489702504532435392851166\ 9703031192611828326620907558270218		
PI-T=.00000000000000000000000000000000724730058949761926019915428752006\ 1805190861699689231348626289014564040		
i=50		
n=3377699720527872		
m=.9999999999999999999999999999999956745860766574258259402067833409964\ 8536431705517478894708057459675646		
x=.0000000000000000186019653227127034638892848244931713466026093694181\ 4794110412790076644858478724760577		
PI-T=.00000000000000000000000000000000181182514737440481504978857188095\ 5878544528324559332568994000613106888		
i=51		
n=6755399441055744		
m=.9999999999999999999999999999999989186465191643564564850516958351906\ 5507355349566828037968547986671625		
x=.000000000000000093009826613563517319446424122475914382989096505665\ 4889879558471872444513739865663141		
PI-T=.0000000000000000000000000000000045295628684360120376244714297029\ 7746340642055753090897592290731058376		
i=52		
n=13510798882111488		
m=.999999999999999999999999999999997296616297910891141212629239587940\ 0962666801340923154135357848017572		
x=.000000000000000046504913306781758659723212061239214397741554460154\ 5881542823246050293453142235034480		
PI-T=.0000000000000000000000000000000011323907171090030094061178574257\ 8110135409975648081223999354120922312		
i=53		
n=27021597764222976		
m=.99999999999999999999999999999999324154074477722785303157309896982\ 7402280948082056797574040765213593		
x=.000000000000000023252456653390879329861606030619764349651653005992\ 5245346792124305334662971001170002		
PI-T=.000000000000000000000000000000002830976792772507523515294643564\ 4757169368014661788507148425091835080		
i=54		
n=54043195528445952		
m=.99999999999999999999999999999999831038518619430696325789327474245\ 5423171127504690824958522772753971		
x=.000000000000000011626228326695439664930803015309901818673435974985\ 6660745318624813184912191409487231		
PI-T=.000000000000000000000000000000000707744198193126880878823660891\ 1203782997575387746550667536168346824		
i=55		
n=108086391056891904		
m=.9999999999999999999999999999999957759629654857674081447331868561\ 3766580337531433745337443979529153		
x=.00000000000000005813114163347719832465401507654953364817669171491\ 5085131649632739163747022966521299		
PI-T=.000000000000000000000000000000000176936049548281720219705915222\ 7802467967666255092599179355538547912		
i=56		
n=216172782113783808		

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log2.octave.out

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```

Eltérés a(z) 1. lépésben: -0.306852819440054714
Eltérés a(z) 2. lépésben: 0.193147180559945286
Eltérés a(z) 3. lépésben: -0.140186152773387973
Eltérés a(z) 4. lépésben: 0.109813847226612027
Eltérés a(z) 5. lépésben: -0.090186152773387929
Eltérés a(z) 6. lépésben: 0.076480513893278701
Eltérés a(z) 7. lépésben: -0.066376628963864204
Eltérés a(z) 8. lépésben: 0.058623371036135796
Eltérés a(z) 9. lépésben: -0.052487740074975364
Eltérés a(z) 10. lépésben: 0.047512259925024614
Eltérés a(z) 11. lépésben: -0.043396830984066326
Eltérés a(z) 12. lépésben: 0.039936502349267045
Eltérés a(z) 13. lépésben: -0.036986574573809938
Eltérés a(z) 14. lépésben: 0.034441996854761459
Eltérés a(z) 15. lépésben: -0.032224669811905193
Eltérés a(z) 16. lépésben: 0.030275330188094807
Eltérés a(z) 17. lépésben: -0.028548199223669912
Eltérés a(z) 18. lépésben: 0.027007356331885668
Eltérés a(z) 19. lépésben: -0.025624222615482695
Eltérés a(z) 20. lépésben: 0.024375777384517350
Eltérés a(z) 21. lépésben: -0.023243270234530322
Eltérés a(z) 22. lépésben: 0.022211275220015092
Eltérés a(z) 23. lépésben: -0.021266985649550096
Eltérés a(z) 24. lépésben: 0.020399681017116533
Eltérés a(z) 25. lépésben: -0.019600318982883502
Eltérés a(z) 26. lépésben: 0.018861219478654934
Eltérés a(z) 27. lépésben: -0.018175817558382046
Eltérés a(z) 28. lépésben: 0.017538468155903653
Eltérés a(z) 29. lépésben: -0.016944290464785960
Eltérés a(z) 30. lépésben: 0.016389042868547365
Eltérés a(z) 31. lépésben: -0.015869021647581638
Eltérés a(z) 32. lépésben: 0.015380978352418362
Eltérés a(z) 33. lépésben: -0.014922051950611914
Eltérés a(z) 34. lépésben: 0.014489712755270445
Eltérés a(z) 35. lépésben: -0.014081715816158136
Eltérés a(z) 36. lépésben: 0.013696061961619654
Eltérés a(z) 37. lépésben: -0.013330965065407319
Eltérés a(z) 38. lépésben: 0.012984824408276863
Eltérés a(z) 39. lépésben: -0.012656201232748798
Eltérés a(z) 40. lépésben: 0.012343798767251224
Eltérés a(z) 41. lépésben: -0.012046445135187822
Eltérés a(z) 42. lépésben: 0.011763078674336014
Eltérés a(z) 43. lépésben: -0.011492735279152400
Eltérés a(z) 44. lépésben: 0.011234537448120308
Eltérés a(z) 45. lépésben: -0.010987684774101947
Eltérés a(z) 46. lépésben: 0.010751445660680647
Eltérés a(z) 47. lépésben: -0.010525150084000234
Eltérés a(z) 48. lépésben: 0.010308183249333136
Eltérés a(z) 49. lépésben: -0.010099980015973009
Eltérés a(z) 50. lépésben: 0.009900019984027009

```

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log2b.octave.out

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```
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```

```
Eltérés a(z) 1. lépésben: -0.306852819440054714  
Eltérés a(z) 10. lépésben: 0.047512259925024614  
Eltérés a(z) 100. lépésben: 0.004975001249750255  
Eltérés a(z) 1000. lépésben: 0.000499750000123034  
Eltérés a(z) 10000. lépésben: 0.000049997499986798  
Eltérés a(z) 100000. lépésben: 0.000004999974964170
```

ápr 14, 02 0:00		rf.out	Page 1/1
j= 1	a=1.0000000000000000	b=1.7500000000000000	x=1.660219213410703
j= 2	a=1.0000000000000000	b=1.660219213410703	x=1.601295972553822
j= 3	a=1.0000000000000000	b=1.601295972553822	x=1.577911477805376
j= 4	a=1.0000000000000000	b=1.577911477805376	x=1.571100496686157
j= 5	a=1.0000000000000000	b=1.571100496686157	x=1.569347471831615
j= 6	a=1.0000000000000000	b=1.569347471831615	x=1.568912399580561
j= 7	a=1.0000000000000000	b=1.568912399580561	x=1.568805432179555
j= 8	a=1.0000000000000000	b=1.568805432179555	x=1.568779194400333
j= 9	a=1.0000000000000000	b=1.568779194400333	x=1.568772762293782
j=10	a=1.0000000000000000	b=1.568772762293782	x=1.568771185705877
j=11	a=1.0000000000000000	b=1.568771185705877	x=1.568770799278268
j=12	a=1.0000000000000000	b=1.568770799278268	x=1.568770704564213
j=13	a=1.0000000000000000	b=1.568770704564213	x=1.568770681349688
j=14	a=1.0000000000000000	b=1.568770681349688	x=1.568770675659783
j=15	a=1.0000000000000000	b=1.568770675659783	x=1.568770674265182
j=16	a=1.0000000000000000	b=1.568770674265182	x=1.568770673923364
j=17	a=1.0000000000000000	b=1.568770673923364	x=1.568770673839584
j=18	a=1.0000000000000000	b=1.568770673839584	x=1.568770673819049
j=19	a=1.0000000000000000	b=1.568770673819049	x=1.568770673814016
j=20	a=1.0000000000000000	b=1.568770673814016	x=1.568770673812783
j=21	a=1.0000000000000000	b=1.568770673812783	x=1.568770673812480
j=22	a=1.0000000000000000	b=1.568770673812480	x=1.568770673812406
j=23	a=1.0000000000000000	b=1.568770673812406	x=1.568770673812388
j=24	a=1.0000000000000000	b=1.568770673812388	x=1.568770673812384
1.568770673812384			

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A1_I_30_121.out

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```

*-----*      MuPAD 2.5.1 -- The Open Computer Algebra System
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*-----*
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>> /*++
&> A1_I_30_121 -- Az Analízis I. példatár I/30. feladatából a 121. megoldása
&>
&> A1_I_30_121 (x,n)
&>
&> x - bemenő x
&> n - bemenő n
&> +*/
>>
>> A1_I_30_121 := proc (x,n)
&> begin
&>   float(cos(x/n)^n);
&>   end_proc;
>>
>> // Példa:
>> A1_I_30_121(0.2, 100);

0.9998000199

>>
>> ///////////////////////////////////////////////////
/
>>
>> /*++
&> A1_I_30_121a -- Az Analízis I. példatár I/30./121. feladat közelítő megoldása
&>
&> A1_I_30_121a (x,h,m)
&>
&> x - bemenő x
&> h - Cauchy-féle hibaküszöb
&> m - maximális lépésszám
&> +*/
>>
>> // Addig növeljük n-et, amíg a sorozat két szomszédos elemének különbsége
>> // nem csökken h alá. (Cauchy-féle konvergenciakritérium.)
>> A1_I_30_121a := proc (x,h,m)
&> local i,v,f,f_e,d;
&> begin
&>   if m<2 then
&>     return(FAIL);
&>   end_if;
&>   i:=1;
&>   v:=TRUE;
&>   while v and i<=m do
&>     f:=A1_I_30_121(x,i);
&>     if i>1 then
&>       d:=float(abs(f-f_e));
&>       if d < h then
&>         v:=FALSE;
&>         end_if; // float...
&>       end_if; // i>1...
&>       i:=i+1;
&>       if v and i<=m then
&>         f_e:=f;

```

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A1_I_30_121.out

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```

&>   end_if;
&>   end_while; // v and...
&>   i:=i-1;
&>   if not v then
&>     print(Unquoted,"Az n=" .expr2text(i-1) . " esetben |f(n+1)-f(n)|<h");
&>   else
&>     print(Unquoted,"Az n=" .expr2text(i-1) . " esetben |f(n+1)-f(n)|=" .
&>       expr2text(d));
&>   end_if;
&>   print(Unquoted,"f(n)=" .expr2text(f_e) . ", f(n+1)=" .expr2text(f));
&>   if not v then
&>     return(f);
&>   else
&>     return(FAIL);
&>   end_if;
&> end_proc;
>>
>> // Példa:
>> A1_I_30_121a(0.5,0.0001,100);

Az n=35 esetben |f(n+1)-f(n)|<h
f(n)=0.9964348203, f(n+1)=0.9965336877
0.9965336877
>> A1_I_30_121a(0.5,0.00001,100);

Az n=99 esetben |f(n+1)-f(n)|=0.00001261056921
f(n)=0.9987381652, f(n+1)=0.9987507757

FAIL
>>
>> ///////////////////////////////////////////////////
/
>>
>> /*++
&> A1_I_30_121b -- Az Analízis I. példatár I/30./121. feladat közelítő megoldása
&>
&> A1_I_30_121a (x,h,m)
&>
&> x - bemenő x
&> h - Cauchy-féle hibaküszöb
&> m - maximális lépésszám
&> +*/
>>
>> // Addig növeljük n-et, amíg a sorozat szomszédos elemének különbsége
>> // nem csökken h alá. (Cauchy-féle konvergenciakritérium.)
>> // Az "a" verzióhoz képest annyit módosítunk, hogy n helyébe 2^n-et írunk.
>> A1_I_30_121b := proc (x,h,m)
&> local i,v,f,f_e,d;
&> begin
&>   if m<2 then
&>     return(FAIL);
&>   end_if;
&>   i:=1;
&>   v:=TRUE;
&>   while v and i<=m do
&>     f:=A1_I_30_121(x,2^i);
&>     if i>1 then
&>       d:=float(abs(f-f_e));
&>       if d < h then

```


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A1_I_30_121.out

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```

&>         v:=FALSE;
&>         end_if; // float...
&>         end_if; // i>1...
&>         i:=i+1;
&>         if v and i<=m then
&>             f_e:=f;
&>             end_if;
&>         end_while; // v and...
&>         i:=i-1;
&>         if not v then
&>             print(Unquoted,"Az n=2^".expr2text(i-1)." esetben |f(2n)-f(n)|<h");
&>         else
&>             print(Unquoted,"Az n=2^".expr2text(i-1)." esetben |f(2n)-f(n)|="
&>                 expr2text(d));
&>             end_if;
&>         print(Unquoted,"f(n)="
&>             .expr2text(f_e)."
&>             , f(2n)="
&>             .expr2text(f));
&>         if not v then
&>             return(f);
&>         else
&>             return(FAIL);
&>         end_if;
&>     end_proc:
>>
>> // Példa:
>> Al_I_30_121b(0.5,0.000000000001,100);

```

$$\text{Az } n=2^{30} \text{ esetben } |f(2n)-f(n)| < h$$

$$f(n)=1.0, f(2n)=1.0$$

$$1.0$$

```

>>
>> ///////////////////////////////////////////////////
/
>>
>> // Ezután számos határérték-számítási feladatot gyorsan meg tudunk oldani:
>> Al_I_39_7 := proc (n)
&> local szorzat,i;
&> begin
&>     szorzat:=1;
&>     for i from 1 to 2*n-1 step 2 do
&>         szorzat:=szorzat*i;
&>     end_for;
&>     return(n/(szorzat^(1/n)));
&> end_proc:
>>
>> // Lusták trükkje:
>> Al_I_30_121 := proc (x,n)
&> begin
&>     float(Al_I_39_7(n));
&> end_proc:
>>
>> // Példa (sajnos, ennél a sorozatnál problémás...):
>> Al_I_30_121b(0.5,0.00001,10);

```

$$\text{Az } n=2^9 \text{ esetben } |f(2n)-f(n)|=0.0004596069263$$

$$f(n)=1.358221437, f(2n)=1.358681044$$

$$\text{FAIL}$$

```

>> quit

```

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A1_I_40_1.out

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```

      *-----*
      /|      |
      *-----*
      | *---|-*
      | /    | /
      *-----*

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>> /*++
>> A1_I_40_1 -- Az Analízis I. példatár I/40. feladatából az 1. megoldása
>>
>> A1_I_40_1 (x,n)
>>
>> x - bemenő x (a feladatban 2)
>> n - bemenő n
>> ++*/
>>
>> A1_I_40_1 := proc (x,n)
>> begin
>>   if n=1 then sqrt(x)
>>   else sqrt(x*A1_I_40_1(x,n-1));
>>   end_if;
>>   end_proc:
>>
>> // Példa:
>> A1_I_40_1(2, 10);

1023/1024
2

>>
>> quit

```

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A1_I_40_3.out

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```

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>> /*++
&> A1_I_40_3 -- Az Analízis I. példatár I/40. feladatából a 3. megoldása
&>
&> A1_I_40_3 (x,n)
&>
&> x - bemenő x (a feladatban c)
&> n - bemenő n
&> ++*/
>>
>> A1_I_40_3 := proc (x,n)
&> begin
&>   if n=1 then sqrt(x)
&>   else sqrt(x+A1_I_40_3(x,n-1));
&>   end_if;
&> end_proc;
>>
>> // Példa:
>> A1_I_40_3(2, 10);

      1/2      1/2      1/2      1/2      1/2      1/2      1/2      1/2
(((((((2      + 2)      + 2)      + 2)      + 2)      + 2)      + 2)      + 2)^
(1/2) + 2)^(1/2)
>> float(%);

1.999997647

>>
>> quit

```

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A1_I_41_1.out

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```

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>> /*++
>> A1_I_41_1 -- Az Analízis I. példatár I/41. feladatából az 1. megoldása
>>
>> A1_I_41_3 (x,n)
>>
>> x - bemenő x
>> n - bemenő n
>> ++*/
>>
>> A1_I_41_1 := proc (x,n)
>> begin
>>     if n=1 then 0
>>     else x+A1_I_41_1(x,n-1)^2;
>>     end_if;
>>     end_proc:
>>
>> // Példa:
>> A1_I_41_1(-2, 10);

                                2

>> float(%);

                                2.0

>>
>> quit

```

feb 22, 03 17:05	A1_I_20.out	Page 1/2
<pre> *-----* / *-----* *-----* / / *-----* MuPAD 2.5.1 -- The Open Computer Algebra System Copyright (c) 1997 - 2002 by SciFace Software All rights reserved. UNREGISTERED VERSION Please contact info@sciface.com to register. >> /*++ &> A1_I_20 -- Az Analízis I. példatár I/20. feladatának megoldása &> &> A1_I_20 (a,m,n) &> &> a - bemenő a &> m - monotonitási irány (1: növekvő, -1: csökkenő) &> n - a vizsgált n-ek maximális száma &> ++*/ >> >> A1_I_20 := proc (a,m,n) &> local v,i,f,f_e; &> begin &> if abs(m) <> 1 or n=1 then &> return(FAIL); &> end_if; &> &> v:=TRUE; &> i:=1; &> while v and (i<=n) do &> f:=i*(a^(1/i)-1); &> print(float(f)); &> if i>1 then &> /* &> * Ha itt nem konvertálunk float-ba, akkor hibaüzenetet &> * kaphatunk, ugyanis csak valós számokat lehet összehasonlítani &> * egymással: &> */ &> if float(f-f_e)*m<0 then v:=FALSE; &> end_if; &> end_if; &> f_e:=f; &> i:=i+1; &> end_while; &> &> i:=i-1; &> if not v then &> i:=i-1; &> end_if; &> if m=-1 then &> print(Unquoted,"Monoton csökkenés n=".expr2text(i)."-ig"); &> else &> print(Unquoted,"Monoton növekedés n=".expr2text(i)."-ig"); &> end_if; &> end_proc; >> >> // Példa: >> A1_I_20(3.5,-1,10);quit </pre>		
	2.5	
	1.741657387	

feb 22, 03 17:05	A1_I_20.out	Page 2/2
<pre> 1.554883458 1.471129599 1.423675786 1.393145575 1.371861719 1.356178365 1.344142968 1.334615817 Monoton csökkenés n=10-ig </pre>		

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sinx.octave.out

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(PI/2)^1/1!=1.570796326794896558
(PI/2)^2/2!=1.233700550136169749
(PI/2)^3/3!=0.645964097506246171
(PI/2)^4/4!=0.253669507901047975
(PI/2)^5/5!=0.079692626246167034
(PI/2)^6/6!=0.020863480763352957
(PI/2)^7/7!=0.004681754135318687
(PI/2)^8/8!=0.000919260274839426
(PI/2)^9/9!=0.000160441184787360
(PI/2)^10/10!=0.000025202042373061
(PI/2)^11/11!=0.000003598843235212
(PI/2)^12/12!=0.000000471087477882
(PI/2)^13/13!=0.000000056921729220
(PI/2)^14/14!=0.000000006386603084
(PI/2)^15/15!=0.000000000668803511
(PI/2)^16/16!=0.000000000065659631
(PI/2)^17/17!=0.000000000006066936
(PI/2)^18/18!=0.000000000000529440
(PI/2)^19/19!=0.000000000000043771
(PI/2)^20/20!=0.000000000000003438
(PI/2)^21/21!=0.000000000000000257
(PI/2)^22/22!=0.000000000000000018
(PI/2)^23/23!=0.000000000000000001
(PI/2)^24/24!=0.000000000000000000
(PI/2)^25/25!=0.000000000000000000

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sinx.out

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```
125.00000
(PI/2)^1/1!=1.57079633
(PI/2)^2/2!=1.23370055
(PI/2)^3/3!=0.64596410
(PI/2)^4/4!=0.25366951
(PI/2)^5/5!=0.07969263
(PI/2)^6/6!=0.02086348
(PI/2)^7/7!=0.00468175
(PI/2)^8/8!=0.00091926
(PI/2)^9/9!=0.00016044
(PI/2)^10/10!=0.00002520
(PI/2)^11/11!=0.00000360
(PI/2)^12/12!=0.00000047
(PI/2)^13/13!=-0.00000017
(PI/2)^14/14!=-0.00000026
(PI/2)^15/15!=-0.00000041
(PI/2)^16/16!=-0.00000064
(PI/2)^17/17!=-0.00000100
(PI/2)^18/18!=-0.00000158
(PI/2)^19/19!=-0.00000248
(PI/2)^20/20!=-0.00000389
```

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expx-horner.octave.out

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GNU Octave, version 2.0.16 (i386-suse-linux-gnu).
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```
n = 20
n=20 T(n)=1.050000000000000044
n=19 T(n)=1.055263157894736903
n=18 T(n)=1.058625730994152025
n=17 T(n)=1.062272101823185322
n=16 T(n)=1.066392006363949152
n=15 T(n)=1.071092800424263247
n=14 T(n)=1.076506628601733073
n=13 T(n)=1.082808202200133296
n=12 T(n)=1.090234016850011090
n=11 T(n)=1.099112183350001049
n=10 T(n)=1.109911218335000171
n=9 T(n)=1.123323468703888883
n=8 T(n)=1.140415433587986138
n=7 T(n)=1.162916490512569512
n=6 T(n)=1.193819415085428215
n=5 T(n)=1.238763883017085732
n=4 T(n)=1.309690970754271433
n=3 T(n)=1.436563656918090404
n=2 T(n)=1.718281828459045091
T(n)=2.718281828459045091
Eltérés: 0.000000000000000000
```


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sinx-hiba.out

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```
125.00000
1!=1, (PI/2)^1/1!=1.57079633
2!=2, (PI/2)^2/2!=1.23370055
3!=6, (PI/2)^3/3!=0.64596410
4!=24, (PI/2)^4/4!=0.25366951
5!=120, (PI/2)^5/5!=0.07969263
6!=720, (PI/2)^6/6!=0.02086348
7!=5040, (PI/2)^7/7!=0.00468175
8!=40320, (PI/2)^8/8!=0.00091926
9!=362880, (PI/2)^9/9!=0.00016044
10!=3628800, (PI/2)^10/10!=0.00002520
11!=39916800, (PI/2)^11/11!=0.00000360
12!=479001600, (PI/2)^12/12!=0.00000047
13!=-2147483648, (PI/2)^13/13!=-0.00000017
14!=-2147483648, (PI/2)^14/14!=-0.00000026
15!=-2147483648, (PI/2)^15/15!=-0.00000041
16!=-2147483648, (PI/2)^16/16!=-0.00000064
17!=-2147483648, (PI/2)^17/17!=-0.00000100
18!=-2147483648, (PI/2)^18/18!=-0.00000158
19!=-2147483648, (PI/2)^19/19!=-0.00000248
20!=-2147483648, (PI/2)^20/20!=-0.00000389
```

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expx.octave.out

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2.72/1!=2.720000000000000195
2.72/2!=1.360000000000000098
2.72/3!=0.453333333333333366
2.72/4!=0.113333333333333341
2.72/5!=0.022666666666666668
2.72/6!=0.003777777777777778
2.72/7!=0.000539682539682540
2.72/8!=0.000067460317460317
2.72/9!=0.000007495590828924
2.72/10!=0.000000749559082892
2.72/11!=0.000000068141734808
2.72/12!=0.000000005678477901
2.72/13!=0.000000000436805992
2.72/14!=0.000000000031200428
2.72/15!=0.000000000002080029
2.72/16!=0.000000000000130002
2.72/17!=0.000000000000007647
2.72/18!=0.000000000000000425
2.72/19!=0.000000000000000022
2.72/20!=0.000000000000000001
2.72/21!=0.000000000000000000
2.72/22!=0.000000000000000000
2.72/23!=0.000000000000000000
2.72/24!=0.000000000000000000
2.72/25!=0.000000000000000000

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sinx2.out

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```
(PI/2)^1/1!=1.570796327000000048
(PI/2)^2/2!=1.233700550458345591
(PI/2)^3/3!=0.645964097759282541
(PI/2)^4/4!=0.253669508033537494
(PI/2)^5/5!=0.079692626298195540
(PI/2)^6/6!=0.020863480779698192
(PI/2)^7/7!=0.004681754139597860
(PI/2)^8/8!=0.000919260275799670
(PI/2)^9/9!=0.000160441184975903
(PI/2)^10/10!=0.000025202042405968
(PI/2)^11/11!=0.000003598843240381
(PI/2)^12/12!=0.000000471087478620
(PI/2)^13/13!=0.000000056921729316
(PI/2)^14/14!=0.000000006386603095
(PI/2)^15/15!=0.000000000668803512
(PI/2)^16/16!=0.000000000065659631
(PI/2)^17/17!=0.000000000006066936
(PI/2)^18/18!=0.000000000000529440
(PI/2)^19/19!=0.000000000000043771
(PI/2)^20/20!=0.000000000000003438
(PI/2)^21/21!=0.000000000000000257
(PI/2)^22/22!=0.000000000000000018
(PI/2)^23/23!=0.000000000000000001
(PI/2)^24/24!=0.000000000000000000
(PI/2)^25/25!=0.000000000000000000
```

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numint.mu.out

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```

*-----*
/|      |
*-----*
|*-----*|
|/      |
*-----*

MuPAD 2.0.0 -- The Open Computer Algebra System

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>> /*
>> * Trapézformula, ld. Móricz Ferenc: Numerikus módszerek az algebrában
>> * és az analízisben, 130. o. illetve Leindler László: Analízis, Nemzeti
>> * könyvkiadó, 1993, 195. o.
>> * A sum eljárás beépített függvény.
>> */
>>
>> Trapez := proc (N)
>> begin
>>   return((b-a)/N*(f(a)/2+f(b)/2+sum(f(a+k*(b-a)/N),k=1..N-1)));
>> end_proc;
>>
>> factor(Trapez(6));

1/12 \ f(a) + f(b) + 2 f \ a b \ + 2 f \ a 2 b \ + 2 f \ 2 a b \ +
      \ 2 2 / + 2 f \ 3 3 / + 2 f \ 3 3 / +
      2 f \ a 5 b \ + 2 f \ 5 a b \ \ (- a + b)
      \ 6 6 / + 2 f \ 6 6 / /

>>
>> Simpson := proc (N)
>> begin
>>   return((b-a)/(6*N)*(f(a)+f(b)+
>>   4*sum(f(a+(2*k+1)*(b-a)/(2*N)),k=0..N-1)+
>>   2*sum(f(a+(2*k)*(b-a)/(2*N)),k=1..N-1)));
>> end_proc;
>>
>> factor(Simpson(3));

1/18 \ f(a) + f(b) + 4 f \ a b \ + 2 f \ a 2 b \ + 2 f \ 2 a b \ +
      \ 2 2 / + 2 f \ 3 3 / + 2 f \ 3 3 / +
      4 f \ a 5 b \ + 4 f \ 5 a b \ \ (- a + b)
      \ 6 6 / + 4 f \ 6 6 / /

>>
>> /*
>> * Romberg-rekurzió
>> */
>>
>> T := proc (k,m)
>> begin
>>   if m=Nil or m=0 then
>>     return(Trapez(k));
>>   end_if;
>>   return((4^m*T(2*k,m-1)-T(k,m-1))/(4^m-1));
>> end_proc;
>>
>> //////////////////////////////////////
//

```

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numint.mu.out

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```

>>
>> f:=sin:
>> a:=0:
>> b:=PI:
>>
>> DIGITS:=20:
>>
>> /*
>> * Határozott integrál számítása (beépített függvény)
>> */
>> int(f(x),x=a..b);

2

>>
>> /*
>> * Illusztráljuk, hogy a trapézformula mennyire lassú konvergenciát ad
>> * (a számolásigény is nagy): 1000-es egyenlő beosztásnál csak 5 tizedesjegy
>> * pontosságot kapunk.
>> */
>>
>> for i from 1 to 3 do
>>   print(float(Trapez(10^i)));
>> end_for;

1.9835235375094545035

1.9998355038874435076

1.9999983550656625709

>>
>> /*
>> * A Simpson-formula lényegesen gyorsabban közelít.
>> */
>>
>> for i from 1 to 3 do
>>   print(float(Simpson(10^i)));
>> end_for;

2.0000067844418011042

2.0000000006764718916

2.00000000000000676452

>>
>> /*
>> * A Romberg-iteráció k=1 esetén már az m=4 esetben 8 jegy pontosságot ad.
>> */
>>
>> for i from 1 to 4 do
>>   print(T(1,i));
>>   print(float(T(1,i)));
>> end_for;

2 PI
----
3

2.0943951023931954923

```

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numint.mu.out

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$$\frac{16 \text{ PI } (2^{1/2} + 1)}{45} - \frac{2 \text{ PI}}{9}$$

1.9985707318238359863

$$\frac{2 \text{ PI}}{135} - \frac{16 \text{ PI } (2^{1/2} + 1)}{135} + \frac{512 \text{ PI } (2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1)}{2835}$$

2.0000055499796705137

$$\frac{16 \text{ PI } (2^{1/2} + 1)}{2025} - \frac{2 \text{ PI}}{8505} - \frac{512 \text{ PI } (2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1)}{8505}$$

$$+ \left(65536 \text{ PI } \left(2 \sin \left(\frac{\text{PI}}{16} \right) + 2 \sin \left(\frac{3 \text{ PI}}{16} \right) + 2 \sin \left(\frac{5 \text{ PI}}{16} \right) + 2 \sin \left(\frac{7 \text{ PI}}{16} \right) + 2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1 \right) \right) / 722925$$

1.9999999945872901717

```
>>
>> /*
>>  * k növelése tovább javítja a konvergencia sebességét.
>> */
>>
>> for i from 1 to 4 do
>>   print(T(2,i));
>>   print(float(T(2,i)));
>> end_for;
```

$$\frac{\text{PI } (2^{1/2} + 1)}{3} - \frac{\text{PI}}{6}$$

2.0045597549844209554

$$\frac{\text{PI}}{90} - \frac{\text{PI } (2^{1/2} + 1)}{9} + \frac{8 \text{ PI } (2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1)}{45}$$

1.9999831309459855992

$$\frac{\text{PI } (2^{1/2} + 1)}{135} - \frac{\text{PI}}{5670} - \frac{8 \text{ PI } (2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1)}{135} +$$

$$\left(256 \text{ PI } \left(2 \sin \left(\frac{\text{PI}}{16} \right) + 2 \sin \left(\frac{3 \text{ PI}}{16} \right) + 2 \sin \left(\frac{5 \text{ PI}}{16} \right) + 2 \sin \left(\frac{7 \text{ PI}}{16} \right) + 2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1 \right) \right) / 722925$$

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numint.mu.out

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$$2 \sin \left(\frac{7 \text{ PI}}{16} \right) + 2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1 \right) \right) / 2835$$

2.00000000162880416574

$$\frac{\text{PI}}{1445850} - \frac{\text{PI } (2^{1/2} + 1)}{8505} + \frac{8 \text{ PI } (2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1)}{2025}$$

$$- \left(256 \text{ PI } \left(2 \sin \left(\frac{\text{PI}}{16} \right) + 2 \sin \left(\frac{3 \text{ PI}}{16} \right) + 2 \sin \left(\frac{5 \text{ PI}}{16} \right) + 2 \sin \left(\frac{7 \text{ PI}}{16} \right) + 2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1 \right) \right) / 8505 +$$

$$\left(32768 \text{ PI } \left(2 \sin \left(\frac{\text{PI}}{16} \right) + 2 \sin \left(\frac{3 \text{ PI}}{16} \right) + 2 \sin \left(\frac{5 \text{ PI}}{16} \right) + 2 \sin \left(\frac{7 \text{ PI}}{16} \right) + 2 \sin \left(\frac{\text{PI}}{32} \right) + 2 \sin \left(\frac{3 \text{ PI}}{32} \right) + 2 \sin \left(\frac{5 \text{ PI}}{32} \right) + 2 \sin \left(\frac{7 \text{ PI}}{32} \right) + 2 \sin \left(\frac{9 \text{ PI}}{32} \right) + 2 \sin \left(\frac{11 \text{ PI}}{32} \right) + 2 \sin \left(\frac{13 \text{ PI}}{32} \right) + 2 \sin \left(\frac{15 \text{ PI}}{32} \right) + 2^{1/2} + (2^{1/2} + 2)^{1/2} + (2 - 2^{1/2})^{1/2} + 1 \right) \right) / 722925$$

1.999999999960339046

```
>>
>> /*
>>  * A Romberg-iteráció "elég gyors".
>> */
>>
>> DIGITS:=50:
>> for i from 1 to 10 do
>>   elteres:=float(2-T(1,i));
>>   tizedesjegy_pontossag:=trunc(abs(trunc(log(10,elteres))));
>>   print(Unquoted, "Pontosság: ");
>>   expr2text(tizedesjegy_pontossag).
>>   " tizedesjegy.");
>> end_for;
```

Pontosság: 1 tizedesjegy.

Pontosság: 2 tizedesjegy.

Pontosság: 5 tizedesjegy.

Pontosság: 8 tizedesjegy.

Pontosság: 11 tizedesjegy.

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numint.mu.out

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Pontosság: 16 tizedesjegy.

Pontosság: 20 tizedesjegy.

Pontosság: 26 tizedesjegy.

Pontosság: 32 tizedesjegy.

Pontosság: 38 tizedesjegy.

>>
>> quit

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Romberg.mu.out

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```

*-----*
/|      |
*-----*|
| *---* |*
| /      | /
*-----*

MuPAD 2.0.0 -- The Open Computer Algebra System

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>> /*
>> * Ez a program szimbolikusan kiszámolja a Romberg-féle integrálásnál
>> * fellépő T(k,m) kifejezéseket. Az eljárást részletesen ld.
>> * Móricz Ferenc: Numerikus módszerek az algebrában és az analízisben c.
>> * könyvében, 136. o.; az ott leírt eljárásnál olvasható jelölés helyett
>> * itt T(k,m) az ottani T(2^m*k,m)-et jelöli.
>> * Copyright (C) Kovács Zoltán, 2002/03/16
>> */
>>
>> T := proc (k,m)
>> begin
>>   if m=Nil or m=0 then
>>     return(procname(k));
>>   end_if;
>>   return((4^m*T(2*k,m-1)-T(k,m-1))/(4^m-1));
>> end_proc:
>>
>> T(k,0);

                                T(k)

>> factor(T(k,1));

                                1/3 (- T(k) + 4 T(2 k))

>> factor(T(k,2));

                                1/45 (T(k) - 20 T(2 k) + 64 T(4 k))

>> factor(T(k,3));

                                1/2835 (- T(k) + 84 T(2 k) - 1344 T(4 k) + 4096 T(8 k))
>> factor(T(k,7));

1/49615367752825875 (- T(k) + 21844 T(2 k) - 95414592 T(4 k) +
99158478848 T(8 k) - 25384570585088 T(16 k) +
1600791219535872 T(32 k) - 24017731997138944 T(64 k) +
72057594037927936 T(128 k))
>> quit

```