The Distribution of Pairs of Points from a Spherical Shell

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We study, via characteristic functions, the distribution of the distance of pairs of points chosen uniformly and independently from a thin spherical shell. The main motivation is that we are interested in the distribution of the expected volume of spindles in d-dimensional models of random ball-polytopes. We determine the density in terms of integrals of Bessel functions using a method of Lord.

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