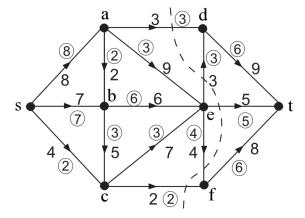
5. Network flows

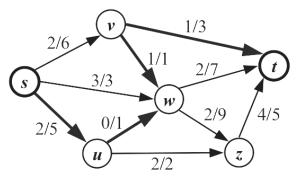
1. Consider the network in the figure (s is the source, t is the sink; and the uncircled numbers denote edge capacities).

- a) Check that the circled numbers define a feasible flow.
- b) Determine the capacity of the [S,T]-cut for $S = \{s, a, b, c, e\}$ and $T = \{d, f, t\}$.
- c) Determine the value of the given flow.
- d) Is this flow value maximal? Justify your answer.

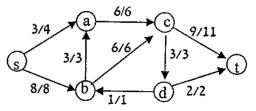


2. Consider the network in the figure.

- a) Check that the first numbers on edges determine a feasible flow.
- b) Check that the path *suwvt* is an augmenting path, and using that, find a feasible flow with greater flow value.
- c) Find a maximum flow in the network, and prove its maximality.



3. Consider the network in the figure (using the conventional notations).



- a) Determine the value of the given flow.
- b) Find an augmenting path, and augment the flow along it.
- c) Is the obtained flow is a maximum flow? (Justify your answer.)

4. (Ford–Fulkerson-algorithm.) Consider the network in the figure (using the conventional notations).

- a) Find an augmenting path, and augment the flow along it.
- b) Repeat the above procedure until you find a maximum flow. Also provide an [S, T]-cut that proves the optimality of the flow.

