

Jordan Structures in Banach Spaces and Symmetric Manifolds

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Abstract

We give an exposition of Jordan structures in Banach spaces and their background in complex holomorphy and symmetric manifolds. We also include some new results and applications to the geometry of Banach spaces.

Contents

- 1 Symmetric Banach Manifolds
 - 1.1 Finite-dimensional symmetric spaces
 - 1.2 Bounded domains and symmetric part of a Banach space
 - 1.3 Symmetric manifolds
- 2 Jordan Structures
 - 2.1 JB^* -triples
 - 2.2 Operator algebras
- 3 Partial Jordan Structure in Banach Spaces
 - 3.1 Isometries and the symmetric part of a Banach space
 - 3.2 Isometries of Banach algebras and the von Neumann inequality
- 4 Some New Results

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